

Real-Time Synthesis Approach for Simultaneous Radar and Spatially Secure Communications from a Common Phased Array

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Abstract — Simultaneous single-aperture radar and communication is an inherently real-time application. Coexistence and spectrum sharing in unpredictable, dynamic 5G environments require the agility of a real-time solution. Physically securing information in communications against recovery by unintended receivers is also of interest. This work describes the computational basis of a real-time system for simultaneous radar and spatially secure communication. Uniform linear array excitation synthesis uses zero-forcing directional modulation and Barker code sequencing. System security and radar performance are simulated and discussed.

Index Terms — Ambiguity function, Barker code, directional modulation, phased array, spectrum sharing.

I. INTRODUCTION

Transmitting simultaneous radar and communications signals from the same system has been suggested as a way of mitigating the spectrum sharing problem [1]. Forming a hybrid system in which both functionalities use the same frequency band can result in more efficient real-time spectrum usage and reduced cost and computation in a joint spatial and spectral regulatory framework [2]. This work extends the directional modulation (DM) concept previously described for secure communications [3]-[5] to a simultaneous radar and spatially secure communications platform. Signals are transmitted in different directions and information can only be recoverable by an intended receiver, based on intelligently computed phase shifts [3].

To integrate radar with communications from the same aperture, Barker code sequencing is applied, as described by Yinjuan [6]. Since Barker code sequences represent discrete versions of continuous signals, they create a powerful link for compressing continuous signals into pulsed radar signals simultaneously. Radar functionality is assessed using the ambiguity function on the return pulse from a moving target, as well as the range resolution and maximum unambiguous detection range.

This work presents a uniform linear array (ULA) system, as shown in Fig. 1. This system can be adapted to various scenarios as described by the work in [7]-[9]. The excitations of each element are derived from a fixed frequency carrier modified by a baseband-weighted vector and applied to subsequent per-element power amplifiers. The baseband-weighted vector is calculated in real-time using zero-forcing directional modulation (ZF) [3]. Since the ZF method is deterministic and presents a reasonable

computational workload, it is suitable for a novel real-time implementation of this proposed system.

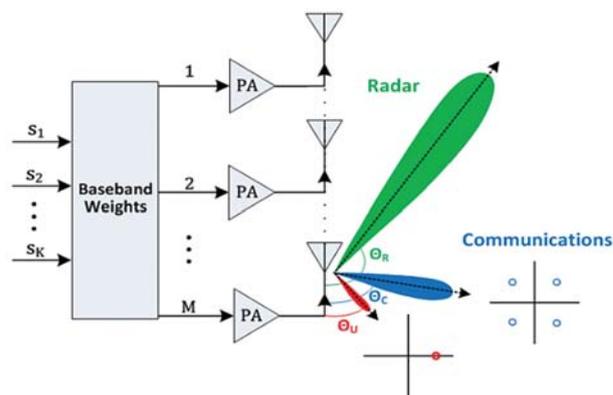


Fig. 1. Block diagram for the simultaneous radar and spatially secure communications ULA transmitter.

II. ZERO-FORCING DIRECTIONAL MODULATION FOR RADAR AND COMMUNICATIONS

The zero-forcing directional modulation problem begins with a description of the linear phased array, the directions of the intended signals with respect to the aperture, the phase of the intended signals, and the relative power allocated to each of the intended signals. The array has M elements uniformly spaced a distance d apart. The number of intended signals is given by the integer K , where $K \leq M$. The directions of the intended signals are collectively referred to as $\boldsymbol{\theta}_d = (\theta_1, \dots, \theta_k, \dots, \theta_K)$, where θ_k is the direction of the k^{th} intended signal. The notation and definitions of the steering vector, steering matrix, and steering matrix pseudo-inverse are defined by Xie [3], respectively. The baseband-weighted vector is given by

$$\mathbf{w} = \frac{\sqrt{P_a}}{\sqrt{p_\Sigma}} (\mathbf{H}(\boldsymbol{\theta}_d)^H)^\dagger \text{diag}\{\sqrt{\mathbf{p}}\} \mathbf{s} \quad (1)$$

where $\mathbf{s} = (s_1, \dots, s_k, \dots, s_K)^T$ is the symbol vector that embodies the phase of the intended signals, $\mathbf{p} = (p_1, \dots, p_k, \dots, p_K)$ is the relative power of the intended signals, p_Σ is the sum of the relative powers, and P_a is the average transmit power. The computed transmit constellation symbols formed in any direction θ' through the phased array antenna beam pattern is then given by

$$\mathbf{S}(\theta', t) = f(\theta) \sum_{n=0}^{N-1} e^{jn(kd\cos\theta - kd\cos\theta')} \mathbf{s}(t) \quad (2)$$

where $\mathbf{s}(t) = |\mathbf{W}|e^{j2\pi f_c t + \angle \mathbf{W}}$ is the time-domain excitation signal formulated by the magnitude and phase shifts computed from the baseband-weighted vector (1) and $f(\theta)$ is the element pattern of the antenna array.

This work demonstrates the novelty of secure real-time multifunctional transmission in multiple real-time synthesis scenarios using the ZF method with the number of antenna elements $M=16$, the element spacing $d = 0.5\lambda$, and the average transmit power $P_a = 1\text{W}$. The radar and communications signals are simultaneously sent from the same phased array with the S-band carrier frequency of 3.6 GHz to lie within the recently reallocated frequency band of 3.55–3.7 GHz. This allows more efficient real-time spectrum usage within the frequency band that has been reallocated for use by both radar and communications platforms which was previously only allocated for use by radar platforms.

A multi-beam transmission pattern is presented. A main beam is sent to 140° that has a magnitude 5 times more powerful than the main beam sent to 30° . These beams represent the radar and communications directional transmissions, respectively. As shown in Fig. 2, a target is present within the radar beam, an intended receiver is present within the communications beam, and an unintended receiver (potential eavesdropper) is present within one of the sidelobes of the multi-beam pattern. A QPSK-modulated communications signal is sent to the intended receiver at 30° . A BPSK-modulated signal is simultaneously sent to the target of interest at 130° which is compressed to a radar pulse upon Barker code sequencing. The unintended receiver at 56.7° consequentially observes these transmissions.

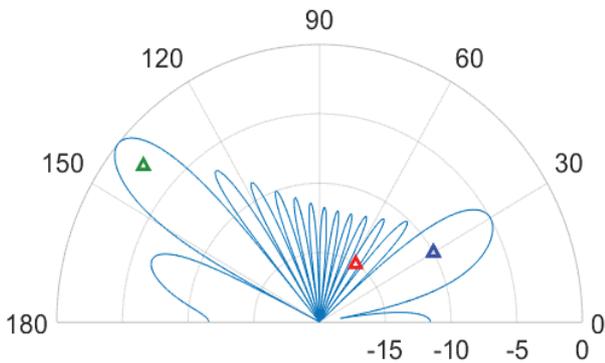


Fig. 2. Phased array spatial scene with a radar beam sent to detect a target (green) at 140° , a communications beam sent to an intended receiver (blue) at 30° , and an unintended receiver (red) located within one of the sidelobes at 56.7° .

In the first transmission signal synthesis scenario, no ZF directional modulation is performed. Without any ZF directional modulation, the unintended receiver has the potential to recover the information sent to the intended receiver. Fig. 3 shows the superposition of constellation symbols for the unintended receiver when no measures are taken to prevent the signal sent to the intended receiver from being recovered in other directions. While the signal for the unintended receiver at 56.7° is affected significantly as shown in Fig. 3, with a potentially sophisticated demodulator, this unintended receiver still has some chance to recover the information.

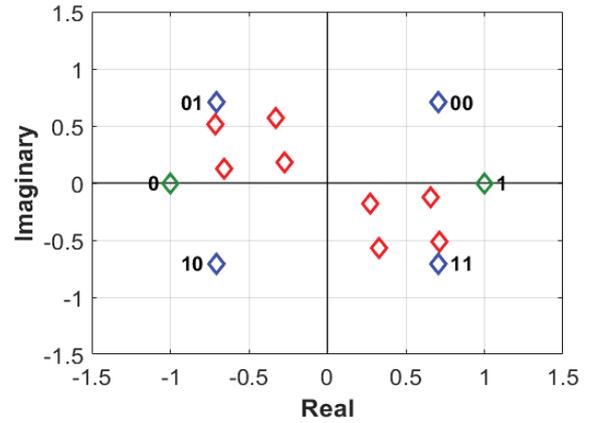


Fig. 3. Radar transmit mode constellation scene with a BPSK-modulated signal sent to 140° (green), and a QPSK-modulated signal sent to an intended receiver at 30° (blue) with an unintended receiver located at 56.7° (red).

The next transmission signal synthesis scenarios are described by Figs. 4 and 5. The DM calculations of the baseband weights using the ZF method are modified to send intentional symbols to the unintended receiver during the transmit (Fig. 4) and receive (Fig. 5) modes of the radar. For baseband-weighted vector calculation, the relative powers are set to $p_1=1$, $p_2=5$, and the sum of the relative powers is set to $p_2=6$ to represent the distribution of power of the phased array beam pattern. In the radar's transmit mode, shown in Fig. 4, spatially secure directional modulation is applied to the same spatial scene as the first scenario, but with the goal of obscuring the signal for the unintended receiver while the radar and intended receiver signals remain undisturbed. In this case, the superposition of the constellation symbols results in a uniform symbol as observed by the unintended receiver at 56.7° in Fig. 4. The Barker coded BPSK constellation is still sent to the radar direction and the intended receiver still observes the QPSK constellation. The functionality of the radar and intended communications signals is therefore left unharmed by the ZF computation. This allows the radar and communications

signal to continue transmitting while ensuring that the unintended receiver does not recover any information.

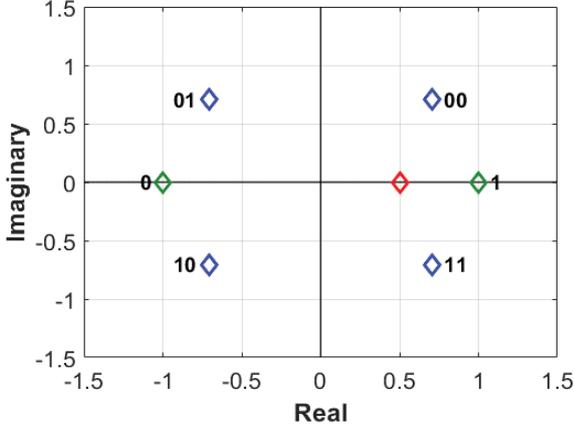


Fig. 4. Radar transmit mode in which zero-forcing directional modulation is used to deliberately send the same symbols to the unintended direction of 56.7° .

Similarly, as shown in Fig. 5, the ZF method is applied to the radar's receive mode where the magnitude of the radar transmission pulse is zero. The baseband weights are recalculated in real-time and still provide the desired constellation symbols to the intended receiver at 30° and the unintended receiver at 56.7° . This ensures spatially secure communications is maintained while the radar continues to transition from the transmit mode to the receive mode and vice-versa according to the structure of the synthesized radar pulse. While intentionally sending a constant symbol to a known unintended receiver direction is one method of ensuring that directional security is maintained, other ZF computations can be applied to accomplish the same goal.

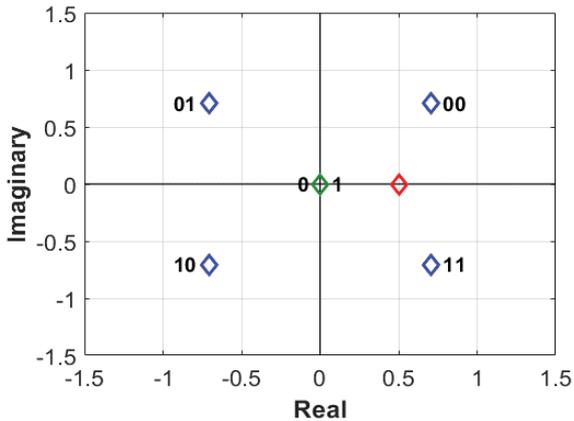


Fig. 5. Radar receive mode in which the ZF method is used to send the same symbols to the unintended receiver at 56.7° .

III. BARKER CODE RADAR SIGNAL SYNTHESIS

To simultaneously synthesize the radar signal to have a transmit and receive mode as proposed in the previous section, N -length phase-coded Barker sequences are applied to compress the continuous BPSK signal into a radar pulse. The BPSK signal is compressed to a radar pulse with a length 2 Barker code, representing the Barker sequence of $+1, -1$. As customary with Barker sequencing, the radar pulse is divided into sub-pulses according to the sequence selected.

A. Range Considerations

A relatively short length Barker code sequence was selected to minimize the radar signal pulse width so that a high bandwidth could be achieved, thus improving the range resolution of the radar signal. A sub-pulse width of $0.25 \mu\text{s}$ was therefore selected for each symbol, resulting in a total pulse width of $0.5 \mu\text{s}$, and a minimum bit rate of 4 Mbps. The communication QPSK constellation is a two-bit signal and thus has a bit rate of 8 Mbps. A pulse repetition interval of $700 \mu\text{s}$ was used to improve the unambiguous range. This repetition interval results in a pulse repetition frequency of $F_{PR} = 1.429 \text{ kHz}$. The return pulse of a moving target traveling at 200 m/s at the distance of 70 km away from the phased array was simulated and is shown in Fig. 6. The unambiguous range (3) and range resolution (4) are calculated as follows, with the speed of light $c = 3 \times 10^8 \text{ m/s}$ and the calculated radar signal bandwidth $B = 2 \text{ MHz}$:

$$R_{unambiguous} = \frac{c}{2F_{PR}} = \frac{3 \times 10^8}{2(1.429 \times 10^3)} = 105 \text{ km} \quad (3)$$

$$\Delta R = \frac{c}{2B} = \frac{3 \times 10^8}{2(2 \times 10^6)} = 75 \text{ m} \quad (4)$$

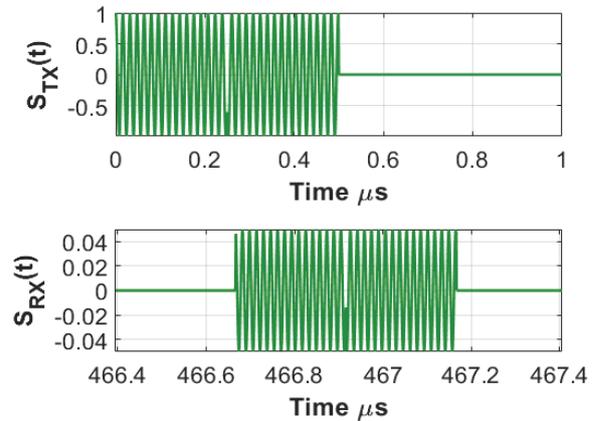


Fig. 6. Barker coded transmission for the radar signal at 140° at 3.6 GHz and its return signal from the moving target.

B. Ambiguity Function

The ambiguity function of the simulated return signal is shown in Fig. 7. To justify acceptable monostatic range radar performance, it is desired that the waveform's ambiguity function contains minimal ambiguity along the range axis, and this goal can be accomplished by using short pulses for the Barker code sequence. The ambiguity function optimization approaches of Eustice [10] may be applicable to optimize the Barker code waveform for different Range/Doppler resolution needs.

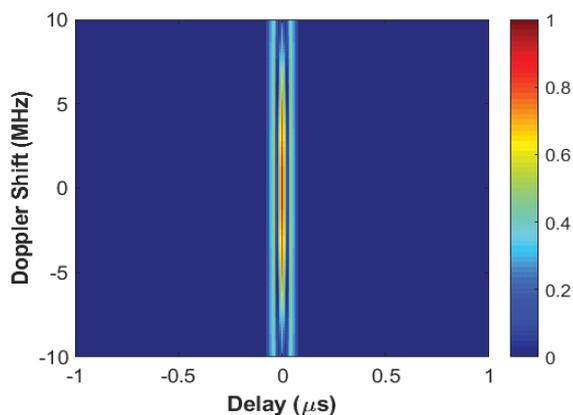


Fig. 7. Ambiguity function for the moving target radar return signal centered at 3.6 GHz in the radar direction of 140°.

IV. CONCLUSIONS

A phased array system that can provide simultaneous radar and spatially secure communications signals has been presented. This work combines directional security concepts from communications into a shared radar and communications framework using a single aperture. The computation of the appropriate phase shifts to apply to the excitation signals on each antenna element to maintain spatial security is significantly reduced. This provides a novel solution for a common phased array that requires suitable radar functionality as well as real-time spatially secure communications. Such a multi-functional system will allow spatial, temporal, and spectral resources to be more efficiently and securely used in the ever-crowded spectral environment.

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REFERENCES

- [1] P. M. McCormick, S. D. Blunt and J. G. Metcalf, "Simultaneous radar and communications emissions from a common aperture, Part I: Theory," *2017 IEEE Radar Conference (RadarConf)*, Seattle, WA, 2017, pp. 1685-1690.
- [2] A. Egbert, C. Latham, C. Baylis and R. J. Marks, "Multi-dimensional coexistence: Using a spatial-spectral mask for spectrum sharing in directional radar and communication," *2018 Texas Symposium on Wireless and Microwave Circuits and Systems (WMCS)*, Waco, TX, 2018, pp. 1-6.
- [3] T. Xie, J. Zhu and Y. Li, "Artificial-Noise-Aided Zero-Forcing Synthesis Approach for Secure Multi-Beam Directional Modulation," in *IEEE Communications Letters*, vol. 22, no. 2, pp. 276-279, Feb. 2018.
- [4] M. P. Daly and J. T. Bernhard, "Directional Modulation Technique for Phased Arrays," in *IEEE Transactions on Antennas and Propagation*, vol. 57, no. 9, pp. 2633-2640, Sept. 2009.
- [5] M. P. Daly and J. T. Bernhard, "Directional modulation and coding in arrays," *2011 IEEE International Symposium on Antennas and Propagation (APSURSI)*, Spokane, WA, 2011, pp. 1984-1987.
- [6] F. Yinjuan, L. Yong, H. Qiongdan and Z. Kunhui, "Design and analysis of LFM/Barker RF stealth signal waveform," *2016 IEEE 11th Conference on Industrial Electronics and Applications (ICIEA)*, Hefei, 2016, pp. 591-595.
- [7] H. Fu, S. Abeywickrama, L. Zhang and C. Yuen, "Low-Complexity Portable Passive Drone Surveillance via SDR-Based Signal Processing," in *IEEE Communications Magazine*, vol. 56, no. 4, pp. 112-118, April 2018.
- [8] Y. Chen, Y. Nijasure, C. Yuen, Y. H. Chew, Z. Ding and S. Boussakta, "Adaptive Distributed MIMO Radar Waveform Optimization Based on Mutual Information," in *IEEE Transactions on Aerospace and Electronic Systems*, vol. 49, no. 2, pp. 1374-1385, April 2013.
- [9] R. C. Daniels and R. W. Heath, "Link Adaptation with Position/Motion Information in Vehicle-to-Vehicle Networks," in *IEEE Transactions on Wireless Communications*, vol. 11, no. 2, pp. 505-509, Feb. 2012.
- [10] D. Eustice, C. Latham, C. Baylis, R. J. Marks and L. Cohen, "Amplifier-in-the-Loop Adaptive Radar Waveform Synthesis," in *IEEE Transactions on Aerospace and Electronic Systems*, vol. 53, no. 2, pp. 826-836, April 2017.